Implementation of linear viscoelasticity model in PDLAMMPS

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1 Introduction

In this documentation the discussion is focused on implementation of linear viscoelasticity model in PDLAMMPS [PLPS08],[Pi95]. The peridynamic viscoelasticity formulation (and its time integration) used in this work was developed by John Mitchell at Sandia National Lab [Mit11]. In the PD-LAMMPS a new pair-peri-style is added in order to incorporate the viscoelasticity. The new source codes pair-peri-ves.cpp and pair-peri-ves.h are introduced. Besides peri-neigh.h are modified for introducing viscoelasticity.

2 Algorithm and implementation

In order to include the viscoelasticity the total extension state can be decomposed into two parts [Mit11].

\footnote{For detail please see the document on implementation of viscoelasticity in state based peridynamics model [Mit11].}
Total extension: \( e(Y) = e^i(Y) + e^d(Y) \) (1)

Volumetric extension: \( e^i(Y) = \frac{\theta(Y)|X|}{3} \) (2)

Deviatoric extension: \( e^d(Y) = |Y| - |X| - \frac{\theta(Y)|X|}{3} \) (3)

Here, \(|Y|, |X|\) and \(\theta\) are the reference state, deformation state and dilation state, respectively. The deviatoric extension can be written as:

\[
e^d(Y) = e^{de}(Y) + e^{db}(i)(Y)
\] (4)

Here, \(e^{de}(Y)\) and \(e^{db}(i)\) are the elastic and back parts of the deviatoric extension. Considering viscoelastic effect the peridynamic force state can be written as:

\[
t = t_i + t^d = -\frac{3p}{m} \omega_x + (\alpha_\infty + \alpha_i) e^d - \alpha_i \omega e^{db}
\] (5)

\(p, k, \alpha_i, t^i\) and \(t^d\) are hydrostatic pressure, bulk modulus, elastic properties volumetric and deviatoric scalar force states, respectively. \(\alpha_\infty + \alpha_i = \frac{15\mu}{m}\); where, \(\mu, m\) are the shear modulus and weighted volume, respectively. The influence function: \(\omega(\xi) = \frac{1}{||\xi||}\), \(||\xi||\) is the scalar reference state. At the current or \(t_{n+1}\) timestep the scalar force state based on LPS is:

\[
t^i_{n+1} = 3k \left( \frac{\theta(i)}{m(i)} \omega_+ + \frac{\theta(i)}{m(i)} \omega_- \right) e\nu(x_j - x_i) V_j
\] (6)

Based on viscoelasticity the deviatoric scale force state can be written as:

\[
t^d_{n+1} = 15 (1 - \lambda) \mu \left( \frac{\omega_+}{m(i)} + \frac{\omega_-}{m(i)} \right) e\nu(x_j - x_i) V_j
\] + \(15\mu \lambda \left( \frac{\omega_+}{m(i)} + \frac{\omega_-}{m(i)} \right) (e - e^{db}_{n+1}) \nu(x_j - x_i) V_j
\] (7)

Here, \(V_j, e^{db}_{n+1}, \nu(x_j - x_i)\) are volume fraction, back extension at current timestep and particle volume scaling factor, respectively. \(\lambda\) varies within zero to one. The back extension at current state can be calculated as:\n
\(^2\text{https://software.sandia.gov/trac/peridigm/}\)
\[ e_{n+1}^{db} = (1 - \text{decay}) e_n^d + \text{decay} \cdot e_n^{db} + \beta \Delta e^d \] (8)

\[ \Delta e^d = e_{n+1}^d - e_n^d \] (9)

\[ \text{decay} = \exp\left(-\frac{dt}{\tau_b}\right) \] (10)

\[ \beta = 1 - \frac{\tau_b}{dt} (1 - \text{decay}) \] (11)

At any current timestep (i.e. \( n + 1 \)), for a bond between \( i^{th} \) and \( j^{th} \) PD nodes, the deviatoric extension is stored on the fly. The value is stored in \text{deviatorextension}[i][j]. Similarly, the back extension is also stored in \text{deviatorBackextension}[i][j]. Both of the arrays initialized with zero.

In the \text{fix_peri_neigh.cpp} an integer flag based switch is used in order to trigger the LPS, PMB or VES (Viscoelastic solid) models. The \text{class} \text{FixPeriNeigh} looks like:

\text{FixPeriNeigh::FixPeriNeigh(LAMMPS \*lmp, int narg, char \*\*arg) : Fix(lmp, narg, arg) }
{

//Get the pair information
Pair \*anypair01 = force->pair_match("peri/pmb",1);
Pair \*anypair02 = force->pair_match("peri/lps",1);
Pair \*anypair03 = force->pair_match("peri/ves",1);

isPMB = 0; \ //Check if PMB
isLPS = 0; \ //Check if LPS
isVES = 0; \ //Check if VES

//Select the flag based on which model is being used
if (anypair01 != NULL)
{
    isPMB=1;
}
else if (anypair02 != NULL)
{
    isLPS=1;
}
else
{
  isVES=1;
}

restart_global = 1;
restart_peratom = 1;
first = 1;

// perform initial allocation of atom-based arrays
// register with atom class
// set maxpartner = 1 as placeholder

maxpartner = 1;
npartner = NULL;
partner = NULL;
if (isVES == 1){
  deviatorextention = NULL;
  deviatorBackextention = NULL;
}

r0 = NULL;
vinter = NULL;
wvolume = NULL;

grow_arrays(atom->nmax);
atom->add_callback(0);
atom->add_callback(1);

// initialize npartner to 0 so atom migration is OK the 1st time

int nlocal = atom->nlocal;
for (int i = 0; i < nlocal; i++) npartner[i] = 0;

// set comm sizes needed by this fix

comm_forward = 1;
There are three integer flags \texttt{isPMB}, \texttt{isLPS}, \texttt{isVES}. PMB, LPS and VES stand for bond based PD model, linear peridynamic solid and viscoelastic peridynamic solid, respectively. Based on the input file any one of these flags are set to one based on:

\begin{verbatim}
Pair *anypair01 = force->pair_match("peri/pmb",1);
Pair *anypair02 = force->pair_match("peri/lps",1);
Pair *anypair03 = force->pair_match("peri/ves",1);
\end{verbatim}

The stored values are used in:

\begin{verbatim}
PairPeriVES::compute(int eflag, int vflag)

double PairPeriVES::single(int i, int j, int itype, int jtype,
                           double rsq, double factor_coul,
                           double factor_lj,double &fforce)
\end{verbatim}

At any current step the total scalar force state \(t\) is calculated and the current deviatoric extension and back extension are stored in order to use in next step. \(\lambda\) and time constant \(\tau_b\) are material dependent parameters. These are defined in the LAMMPS input script. This will be discussed in the next section. The new LAMMPS pair style \{pair\_peri\_ves\} is defined with addition arguments in the input file (\(\lambda\) and \(\tau_b\)):

\begin{verbatim}
void PairPeriVES::settings(int narg, char **arg)
{
    if (narg) error->all(FLERR,"Illegal pair_style command");
}

/* ----------------------------------------------------------------------
set coeffs for one or more type pairs
------------------------------------------------------------------------- */

void PairPeriVES::coeff(int narg, char **arg)
{
    if (narg != 9) error->all(FLERR,"Incorrect args for pair coefficients");
    if (!allocated) allocate();
\end{verbatim}
int ilo,ihi,jlo,jhi;
force->bounds(arg[0],atom->ntypes,ilo,ihi);
force->bounds(arg[1],atom->ntypes,jlo,jhi);

double bulkmodulus_one = atof(arg[2]);
double shearmodulus_one = atof(arg[3]);
double cut_one = atof(arg[4]);
double s00_one = atof(arg[5]);
double alpha_one = atof(arg[6]);
double mlambda_one = atof(arg[7]); // New
double mtaui_one = atof(arg[8]); // New

int count = 0;
for (int i = ilo; i <= ihi; i++) {
  for (int j = MAX(jlo,i); j <= jhi; j++) {
    bulkmodulus[i][j] = bulkmodulus_one;
shearmodulus[i][j] = shearmodulus_one;
cut[i][j] = cut_one;
s00[i][j] = s00_one;
alpha[i][j] = alpha_one;
m_lambda[i][j] = mlambda_one; // New
m_taubi[i][j] = mtaui_one; // New
setflag[i][j] = 1;
count++;
  }
}

if (count == 0) error->all(FLERR,"Incorrect args for pair coefficients");
}

3 LAMMPS command for PD VES

There is no significant change in the LAMMPS input script for viscoelastic model. For PD VES the LAMMPS commands are:

pair_style peri/ves
pair_coeff i j Bulk_modulus Shear_modulus s00 alpha lambda tau
The LAMMPS compilation with the VES is same. The updated `Install.sh` should be used.

4 Conclusion

The LAMMPS implementation of peridynamic viscoelastic model is still in beta phase. Any bug or issue can be informed to the authors through rezwanur.rahman@utsa.edu.

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References

