



# Using Ray Tracing to Model Thermal Radiation in LIGGGHTS

Stefan Amberger  
Christoph Kloss, Stefan Pirker

CD Laboratory on Particulate Flow Modelling  
Johannes Kepler University Linz, Austria

August 7-8, 2013



- 1 The Model
- 2 Implementation Details
- 3 Verification
- 4 Examples



- 1 The Model
- 2 Implementation Details
- 3 Verification
- 4 Examples



# Model - Depiction

A sketch of ray tracing

- Red sphere emits a ray that is reflected twice and heats up blue sphere.
- Blue sphere emits ray that hits background and leads to heat transfer from the background.
- Gray arrows are normal vectors.

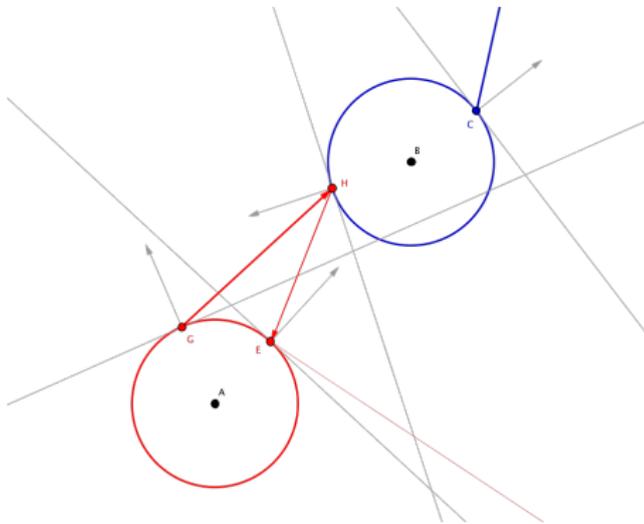


Figure 1: Depiction of radiation of two spheres.



based on the idea of raytracing and Stefan Boltzmann's law.

### Simplifying Assumptions

- homogeneous temperature of particles:

rays originate on points  $\sim U(\text{surface of particle})$

- instantaneous heat transfer within particle (particle has *one* temperature)
- purely diffuse surfaces (for the moment)
  - angle of reflection  $\sim U(-\pi/2, \pi/2) \times U(-\pi/2, \pi/2)$
  - no refraction
- emissivity is constant across all wavelengths
- correctness of Stefan Boltzmann's law
- constant background radiation



# Model - Description

## Algorithm for One Timestep

---

for each particle  $i$ :

- generate random point on particle
- generate random direction (pointing to outside of particle  $i$ )
- calculate heat flux using Stefan Boltzmann's law:  $\dot{Q}_i = \epsilon_i \sigma A_i T_i^4$
- decrease heat flux of particle  $i$  by  $\dot{Q}_i$
- trace ray for intersections with other particles
- if (intersection with particle  $j$ ):
  - transfer absorbed part of heat:  $\dot{Q}_i \epsilon_j$
  - generate random direction (that points outside of particle  $j$ )
  - shoot new reflection ray with  $\dot{Q}_j = (1 - \epsilon_j) \dot{Q}_i$  (recursively, up to depth  $N$ )
- else (assume background radiation):
  - increase heat flux of particle  $i$  by  $\epsilon_i \sigma A_i T_{\text{background}}^4$



# Model - Description

## Formal Description - Definitions

### Definition 1 (used sets)

Let  $I$  be the set of particles,  $\emptyset$  the background with temperature  $T_{\emptyset}$  and  $U := \{\emptyset, I\}$ .

### Definition 2 (general symbols)

For a particle  $i$  let  $T_i$  denote its temperature,  $A_i$  its surface area and  $\epsilon_i$  its emissivity. Furthermore let  $\sigma$  be Stefan Boltzmann's constant.

### Definition 3 (relation symbols)

- $\forall i \in I, j \in U : i \rightsquigarrow j$   
 $\iff$  a ray that was cast from  $i$  hit or has been reflected to  $j$ .
- $\forall i, k \in I, j \in U : i \overset{k}{\rightsquigarrow} j$   
 $\iff i \rightsquigarrow j \wedge$  the ray from  $i$  was reflected via  $k$ .
- $\forall i \in I, j \in U : N_{i \rightsquigarrow j}$  is the number of reflections from  $i$  to  $j$



# Model - Description

## Formal Description - Model

Using Iverson bracket notation and definitions 1, 2 and 3 the heat flux of a particle  $i \in I$  is in this model defined as follows:

### Heat Flux of Particle $i \in I$

$$\dot{Q}_i := -\epsilon_i \sigma A_i T_i^4 \quad (1)$$

$$+ \epsilon_i \sum_{\substack{j \in I \\ j \rightsquigarrow i}} (\epsilon_j \sigma A_j T_j^4 \prod_{\substack{k \in I \\ j \overset{k}{\rightsquigarrow} i}} (1 - \epsilon_k)) \quad (2)$$

$$+ [i \rightsquigarrow \emptyset] \epsilon_i \sigma A_i T_{\emptyset}^4 \prod_{\substack{k \in I \\ i \overset{k}{\rightsquigarrow} \emptyset}} (1 - \epsilon_k) \quad (3)$$

$$+ \epsilon_i \sigma A_i T_i^4 \prod_{\substack{j, k \in I \\ N_{i \rightsquigarrow j} > N_{\max} \vee \prod_{i \overset{k}{\rightsquigarrow} j} (1 - \epsilon_k) < 0.001}} (1 - \epsilon_k) \quad (4)$$



- (1): Heatloss due to cooling

$$-\epsilon_i \sigma A_i T_i^4$$

- (2): Particle to particle heat transfer due to radiation (including reflection)

$$+\epsilon_i \sum_{\substack{j \in I \\ j \rightsquigarrow i}} (\epsilon_j \sigma A_j T_j^4 \prod_{\substack{k \in I \\ j \rightsquigarrow k \\ k \rightsquigarrow i}} (1 - \epsilon_k))$$



- (1): Heatloss due to cooling

$$-\epsilon_i \sigma A_i T_i^4$$

- (2): Particle to particle heat transfer due to radiation (including reflection)

$$+\epsilon_i \sum_{\substack{j \in I \\ j \rightsquigarrow i}} (\epsilon_j \sigma A_j T_j^4 \prod_{\substack{k \in I \\ j \overset{k}{\rightsquigarrow} i}} (1 - \epsilon_k))$$



- (3): Background radiation

$$+[i \rightsquigarrow \emptyset] \epsilon_i \sigma A_i T_\emptyset^4 \prod_{\substack{k \in I \\ i \rightsquigarrow^k \emptyset}} (1 - \epsilon_k)$$

- (4): Residuum that arises due to cut-off of possibly infinite geometric series of reflections

$$+\epsilon_i \sigma A_i T_i^4 \prod_{\substack{j, k \in I \\ N_{i \rightsquigarrow j} > N_{\max} \vee \prod_{i \rightsquigarrow^k j} (1 - \epsilon_k) < 0.001}} (1 - \epsilon_k)$$



- (3): Background radiation

$$+[i \rightsquigarrow \emptyset] \epsilon_i \sigma A_i T_{\emptyset}^4 \prod_{\substack{k \in I \\ i \rightsquigarrow^k \emptyset}} (1 - \epsilon_k)$$

- (4): Residuum that arises due to cut-off of possibly infinite geometric series of reflections

$$+\epsilon_i \sigma A_i T_i^4 \prod_{\substack{j, k \in I \\ N_{i \rightsquigarrow j} > N_{\max} \vee \prod_{i \rightsquigarrow^k j} (1 - \epsilon_k) < 0.001}} (1 - \epsilon_k)$$



- 1 The Model
- 2 Implementation Details**
- 3 Verification
- 4 Examples



LIGGGHTS allows to integrate scalar and vectorial properties.  
e.g. initial temperature at  $t_0$  + heat flux  $\leadsto$  temperature at  $t_1$

$\implies$  suffices to calculate radiative heat transfer, integration is handled by LIGGGHTS



- 2 Implementation Details
  - Usage of neighborlists
  - Parallelization

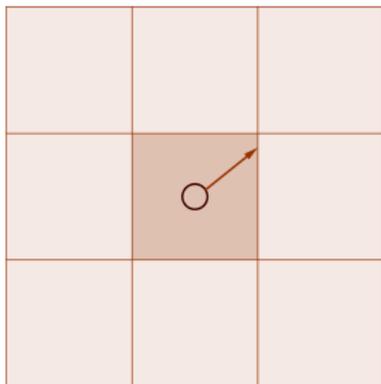


Don't check all particles for each ray.

- 1 Check all neighbors of emitting particle
- 2 Walk the neighbor-list-bins in the respective direction

# Usage of neighbor-lists

## Example

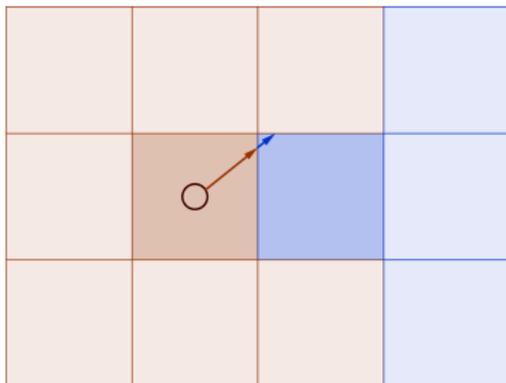


**Figure 2:** Check atoms of full stencil

Check for intersections, then find next central bin.

# Usage of neighbor-lists

## Example

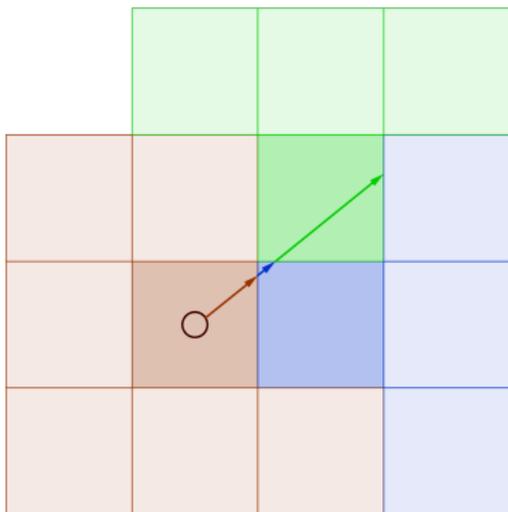


**Figure 3:** Check particles in new bins only (light blue)

Check for intersections, then find next central bin.

# Usage of neighbor-lists

## Example

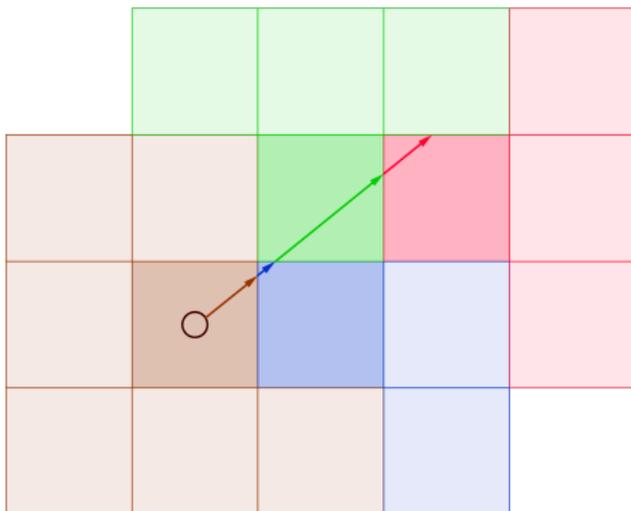


**Figure 4:** Check particles in new bins only (light green)

Check for intersections, then find next central bin.

# Usage of neighbor-lists

## Example



**Figure 5:** Check particles in new bins only (light red)

Check for intersections, then find next central bin.



## 2 Implementation Details

- Usage of neighborlists
- Parallelization



Heat transfer obeys inverse square law, thus we can

- introduce *maximum radiation-distance* to ignore “negligible” long distance contributions
- use maximum radiation-distance as “force” cutoff (`cutghost`) of radiation fix
- invoke forward / backward communication of heat-flux; use LIGGGHTS built-in parallelism



- 1 The Model
- 2 Implementation Details
- 3 Verification**
- 4 Examples



## Bulk-behavior of a box of particles

- temperature adjusts to surrounding temperature
- corners cool off faster than surfaces
- visible temperature gradient within the bulk (inside: hot, outside: cools)



- radiative cooling of a single sphere
  - temperature after a certain time
  - comparison with direct forward Euler integration of Stefan Boltzmann's law

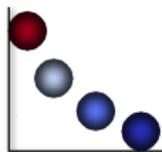


Figure 6: Radiative cooling of a single sphere.

- radiative heat transfer between two large, parallel planes  
(see [1], p. 821, Example 2)

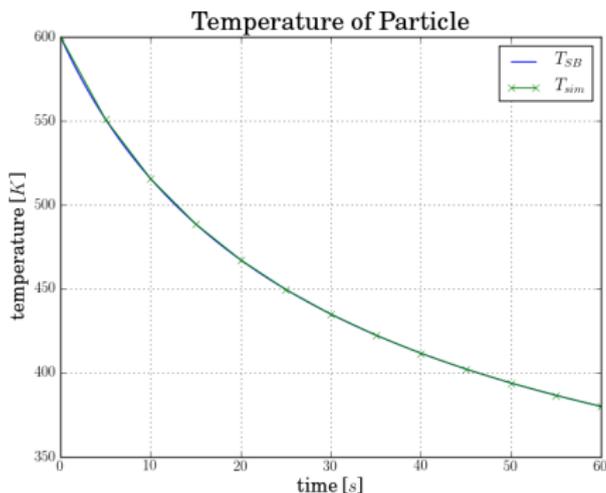


Figure 7: Radiative heat transfer between two parallel planes.

- 1 *VDI Wärmeatlas*, vol. 7, Verein Deutscher Ingenieure VDI-Gesellschaft Verfahrenstechnik und Chemieingenieurwesen (GVC), (german), 1994

# Quantitative Correctness

## Radiative Cooling of a Single Sphere - Results



**Figure 8:** Temperature of integrated Stefan Boltzmann law vs. simulation using our radiation model.

⇒ Model represents Stefan Boltzmann's law for a single particle.

# Quantitative Correctness

## Two Parallel Planes - Analytical Setup

Setup of the analytical solution:

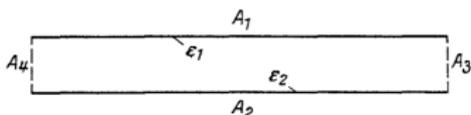


Figure 9: Setup of solution [1]

Analytical representation of heat transfer for this setup:

$$\dot{Q} = \frac{\sigma A}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1} \cdot (T_1^4 - T_2^4)$$

- Simplification: No interaction with environment, no heat is lost due to cooling.
- Exaggerated heat conduction within the plates

**1** VDI *Wärmeatlas*, vol. 7, Verein Deutscher Ingenieure VDI-Gesellschaft Verfahrenstechnik und Chemieingenieurwesen (GVC), (german), 1994



Figure 10: Radiative heat transfer between two parallel planes.

# Quantitative Correctness

## Two Parallel Planes - Results

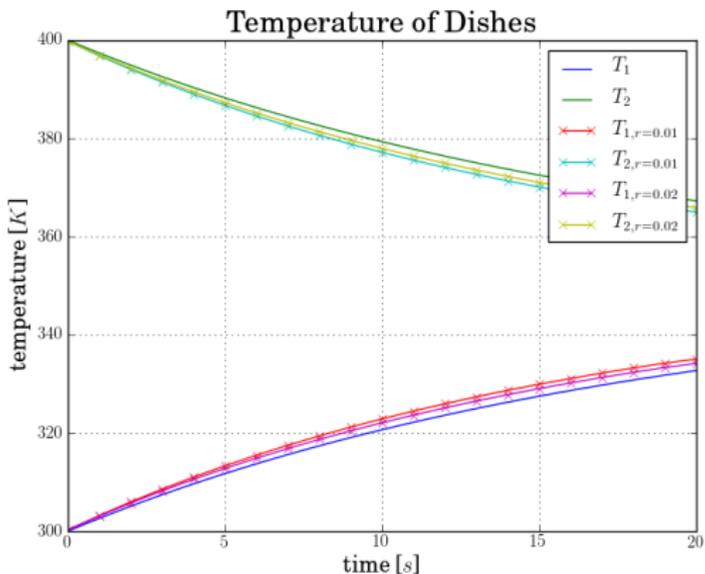


Figure 11: Temperature of both plates for 20 seconds and varying Radius.

# Quantitative Correctness

## Two Parallel Planes - Results Explained



Small error of about 1% after 20 seconds, due to

- Grey particles (area correction calculated for black only)
- differing surface structure of flat planes vs. particulate planes.

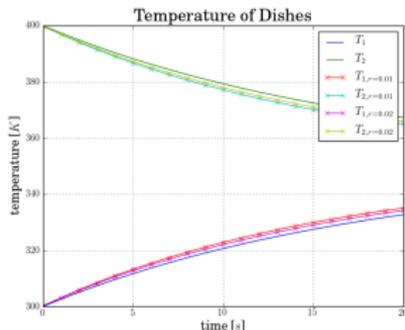
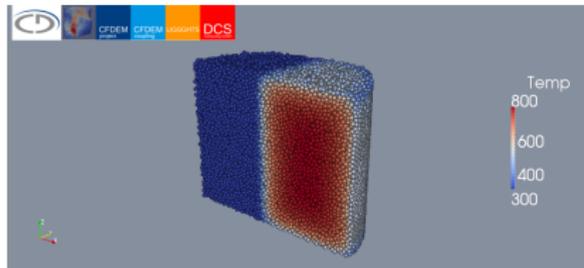


Figure 12: Temperature of both plates.



- 1 The Model
- 2 Implementation Details
- 3 Verification
- 4 Examples**



**Animation 1:** Slice of particle-bed.

Simulation of radiative heat transfer of 110.000 particles on 16 cores.

- Particle radius: 2mm
- Cylinder:
  - Diameter: 70cm
  - Height: 2.8m
  - Vol. Frac.: 30%
- Walltime: 38 h
- CPUtime: 608 h
- simulated realtime: 25 sec



- [1] *VDI Wärmeatlas*, vol. 7, Verein Deutscher Ingenieure VDI-Gesellschaft Verfahrenstechnik und Chemieingenieurwesen (GVC), (german), 1994.



Thank you.  
Questions?

Johannes Kepler University Linz  
CD Laboratory on Particulate Flow Modelling

Contact:  
[stefan.amberger@jku.at](mailto:stefan.amberger@jku.at)